

CMPE353/CMSE354

RELATIONAL DATABASE DESIGN EXAMPLES

(Ch. 8)

Problem at hand

We will consider the following set F of functional dependencies for relation schema $R = (A, B, C, D, E)$ throughout these examples.

$$F = \{A \rightarrow BC, CD \rightarrow E, B \rightarrow D, E \rightarrow A\}$$

Ex. 1 Compute B^+

- Using the attribute closure algorithm below, we find that $B^+=BD$

$$F = \{A \rightarrow BC, CD \rightarrow E, B \rightarrow D, E \rightarrow A\}$$

```
result :=  $\alpha$ ;  
  while (changes to result) do{  
    for each  $\beta \rightarrow \gamma$  in  $F$  do  
      begin  
        if  $\beta \subseteq \textit{result}$  then  
  
           $\textit{result} := \textit{result} \cup \gamma$   
        end  
      }  
  }
```

$\alpha^+ = \textit{result}$

result=B
result=BD

$B^+=BD$

Remember! This means that the functional dependencies $B \rightarrow B$, $B \rightarrow D$ and $B \rightarrow BD$ are all in F^+

Ex.2 Is BC a candidate key for R?

- Using the attribute closure algorithm we find that $(BC)^+ = ABCDE$

Since the closure contains all attributes in R, **BC is a superkey.**

- Now, we test if any subset of BC, that is B or C is a superkey for R?
If not, BC will be a candidate key.

- We already know from Ex.1 that $B^+ = BD$, so B is not a SK.
- Using attribute closure algorithm, we find that $C^+ = C$, so C is not a SK.
- **Since no subset of BC is SK, BC becomes the candidate key!**

Additional information.

- We can show that *A*, *BC*, *CD*, and *E* are all **candidate keys** for R.
- Try this!

Ex. 3 Let $R1 = (A, B, C)$, $R2 = (A, D, E)$. Is this decomposition of R lossless join decomposition?

- We know that a decomposition $\{R1, R2\}$ is a lossless-join decomposition if $R1 \cap R2 \rightarrow R1$ or $R1 \cap R2 \rightarrow R2$.

(In other words if $R1 \cap R2$ is a **superkey** for R1 or R2)

- $R1 \cap R2 = A$
- We know from slide 5, that A is superkey for R, so it must be a superkey for any decomposition of R. (R1 and R2 in this case)
- **So the decomposition is lossless join.**
- Alternatively;
 - Use the only functional dependency (FD) in F defined over R1: $A \rightarrow BC$
 - Compute $A^+ = ABC$. Since all attributes of R1 are in A^+ , A is a SK for R1.

Ex.4 Is $R = (A, B, C, D, E)$ in BCNF given $F = \{A \rightarrow BC, CD \rightarrow E, B \rightarrow D, E \rightarrow A\}$?

A relation schema R is in BCNF with respect to a set F of functional dependencies if for all functional dependencies in F of the form

$$\alpha \rightarrow \beta$$

where $\alpha \subseteq R$ and $\beta \subseteq R$, at least one of the following holds:

1) $\alpha \rightarrow \beta$ is trivial (i.e., $\beta \subseteq \alpha$)

OR

2) α is a superkey for R

Ex. 4 Solution Continued

- $F = \{A \rightarrow BC, CD \rightarrow E, B \rightarrow D, E \rightarrow A\}$

We must check each FD to see if it satisfies cond. 1 or 2.

- If they all satisfy, then R is BCNF.
 - Checking $A \rightarrow BC$; we know that A is a SK for R (slide 5); 2 is satisfied.
 - Checking $CD \rightarrow E$; we know that CD is a SK for R (slide 5); 2 is satisfied.
 - Checking $B \rightarrow D$; B is not SK and is non-trivial. Both 1 and 2 are not satisfied.
 - Checking $E \rightarrow A$; we know that E is a SK for R (slide 5); 2 is satisfied.

Since we found at least one FD in F which doesn't satisfy any of the conditions, we conclude that **R is not BCNF**.

Ex.5 Use BCNF decomposition algorithm once to decompose R in Ex.4 into R_1 and R_2 .

- We decompose R into: assume $(\alpha \rightarrow \beta)$
 $R_1 = (\alpha \cup \beta)$, $R_2 = (R - (\beta - \alpha))$ using the functional dependency which violates BCNF.
 - In Ex.4 $B \rightarrow D$ was the violating FD, so;
 - $R_1 = (\alpha \cup \beta) = (B \cup D) = (B, D)$
 - $R_2 = (R - (\beta - \alpha)) = (ABCDE) - (D - B) = (A, B, C, E)$
 - *(Do not check if this decomposition is BCNF since this requires all FD in the closure of F , which we do not know!)*

Ex.6 Is $R = (A, B, C, D, E)$ in 3NF given $F = \{A \rightarrow BC, CD \rightarrow E, B \rightarrow D, E \rightarrow A\}$?

- A relation schema R is in **third normal form (3NF)** if for all:

$$\alpha \rightarrow \beta \text{ in } F^+$$

at least one of the following holds:

- 1) $\alpha \rightarrow \beta$ is trivial (i.e., $\beta \in \alpha$)
- 2) α is a superkey for R
- 3) Each attribute A in $\beta - \alpha$ is contained in a candidate key for R .
(**NOTE:** each attribute may be in a different candidate key)

Ex. 6 solution continued

- We know from Ex.4 that FDs $A \rightarrow BC$, $CD \rightarrow E$, $E \rightarrow A$ all satisfy condition 2. But the FD $B \rightarrow D$ doesn't satisfy 1 or 2. We check if it satisfies condition 3.
- 3) Each attribute A in $\beta - \alpha$ is contained in a candidate key for R

$$\beta - \alpha = D - B = D$$

So we check if attribute D is in any candidate key for R . We know that CD is a candidate key for R (slide 5). Therefore D is contained in candidate key CD . So condition 3 is satisfied.

- We conclude that R is 3NF.
- Nevertheless we can still give a 3NF decomposition of R (Ex.7 next)

Ex.7 Give a 3NF decomposition of $R=(A,B,C,D,E)$ given $F=\{A \rightarrow BC, CD \rightarrow E, B \rightarrow D, E \rightarrow A\}$

- A simplified version of the 3NF decomposition may be written in the following way:
- **Step 1) For each FD $\alpha \rightarrow \beta$ in F create a $R_i=(\alpha,\beta)$**
 - Using every FD in F we get: $R_1=(ABC), R_2=(CDE), R_3=(BD), R_4=(AE)$
- **Step 2) If none of the previously formed schemas contains a candidate key for R , form an additional R_j to include one of the candidate keys.**
 - Since several candidate keys (not just one) are included in R_1, R_2, R_3, R_4 we do not need to form an additional R_5 .
- **Step 3) If any schema R_j is contained in another schema R_k previously formed, remove schema R_j**
 - Here we have no such schema, so we do not remove any.
- We conclude that, $R_1=(ABC), R_2=(CDE), R_3=(BD), R_4=(AE)$ is a 3NF decomposition of R .
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Ex.8 Given $F = \{A \rightarrow BC, CD \rightarrow E, B \rightarrow D, E \rightarrow A\}$ determine i) if attribute C in $CD \rightarrow E$ is extraneous ii) if attribute B in $A \rightarrow BC$ is extraneous

- We use the following tests to check for extraneous attributes:
- **Left hand side attribute test:**
- To test if attribute $A \in \alpha$ is extraneous in α compute $(\{\alpha\} - A)^+$ using the dependencies in F
 1. check that $(\{\alpha\} - A)^+$ contains β ; if it does, A is extraneous in α
- **Right hand side attribute test:**
- To test if attribute $A \in \beta$ is extraneous in β
 1. compute α^+ using only the dependencies in $F' = (F - \{\alpha \rightarrow \beta\}) \cup \{\alpha \rightarrow (\beta - A)\}$,
 2. check that α^+ contains A ; if it does, A is extraneous in β

Ex. 8 solution continued

i) is attribute C in $CD \rightarrow E$ is extraneous ?

- Apply LHS and compute $CD - C = D^+$ using F by attribute closure algorithm.
- $D^+ = D$.
- Since it doesn't contain all attributes on the RHS (i.e. attribute E), we conclude that C is not extraneous.

Ex. 8 solution continued

ii) is attribute B in $A \rightarrow BC$ is extraneous?

- Apply RHS and compute A^+ using F' by attribute closure algorithm.
- $F' = \{A \rightarrow C, CD \rightarrow E, B \rightarrow D, E \rightarrow A\}$
- $A \rightarrow BC$ is replaced by $A \rightarrow C$ (i.e. Remove the attribute under test from the FD it belongs to; leave all others unchanged).
- $A^+ = AC$
- Since it doesn't contain attribute under test (i.e attribute B) we conclude that B is not extraneous.