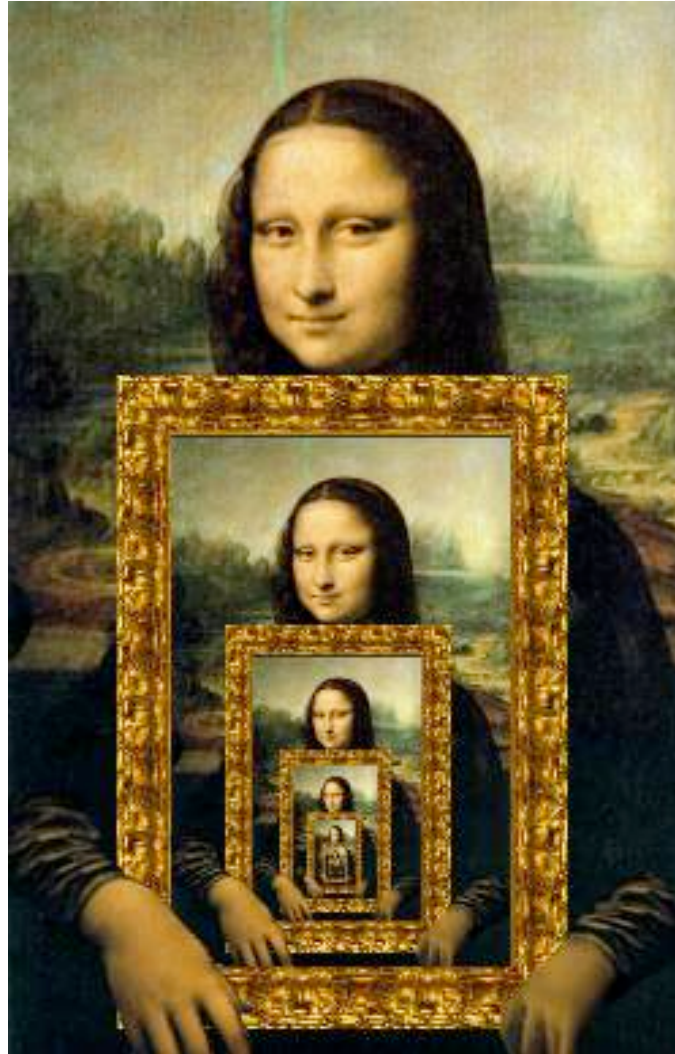


# Chapter 3: Recursion

---

- Theory
  - Introduce recursive definitions in Prolog
  - Go through four examples
  - Show that there can be mismatches between the declarative and procedural meaning of a Prolog program
- Exercises
  - Exercises of LPN chapter 3
  - Practical work

# Chapter 3: Recursion

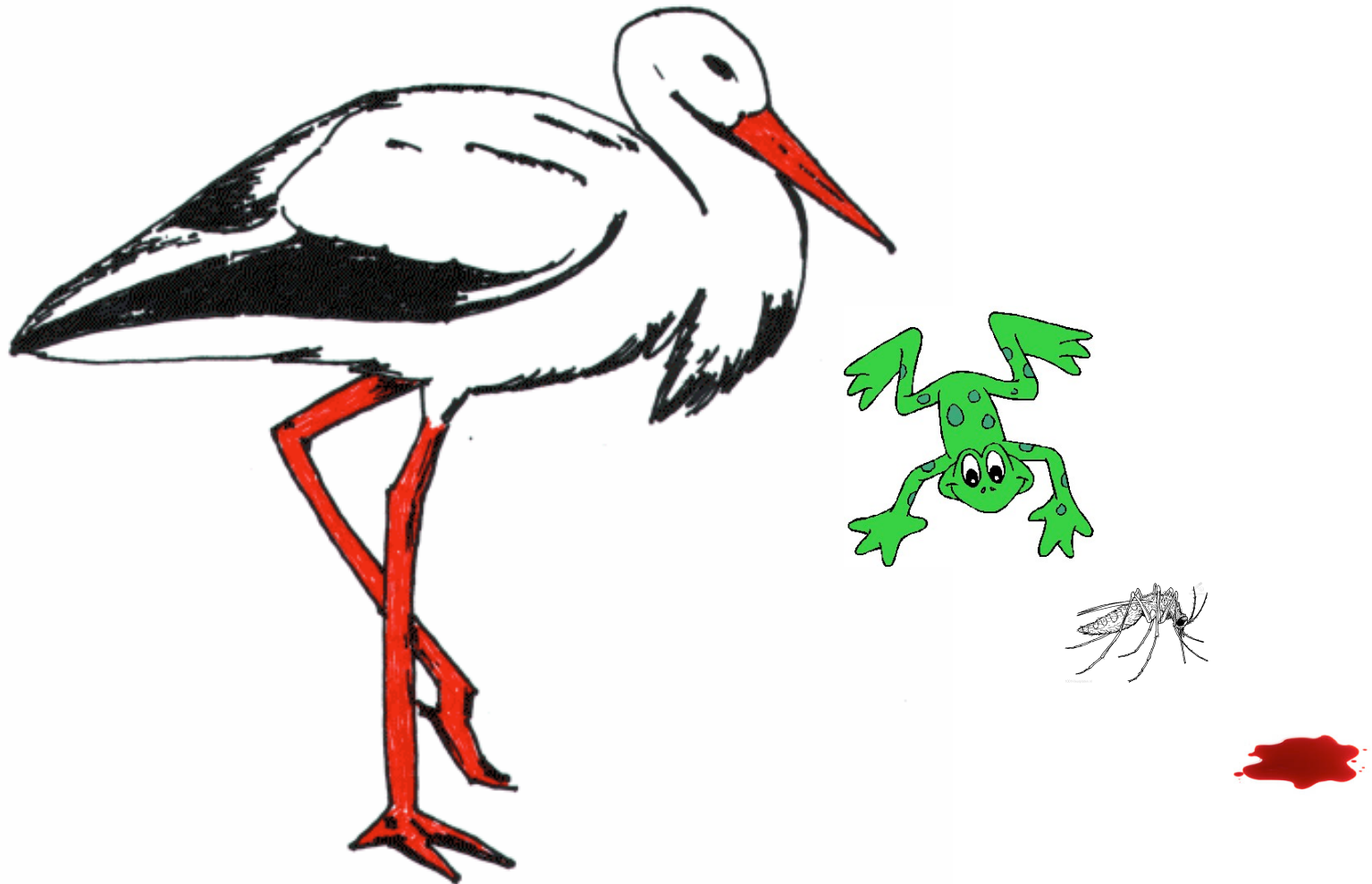


# Recursive definitions

---

- Prolog predicates can be defined recursively
- A predicate is recursively defined if one or more rules in its definition refers to itself

# Example 1: Eating



# Example 1: Eating

```
isDigesting(X,Y):- justAte(X,Y).
```

```
isDigesting(X,Y):- justAte(X,Z), isDigesting(Z,Y).
```

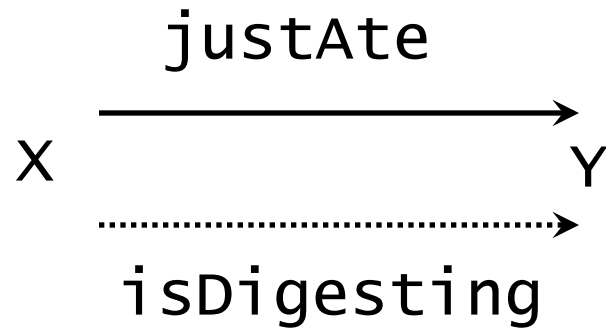
```
justAte(mosquito,blood(john)).
```

```
justAte(frog,mosquito).
```

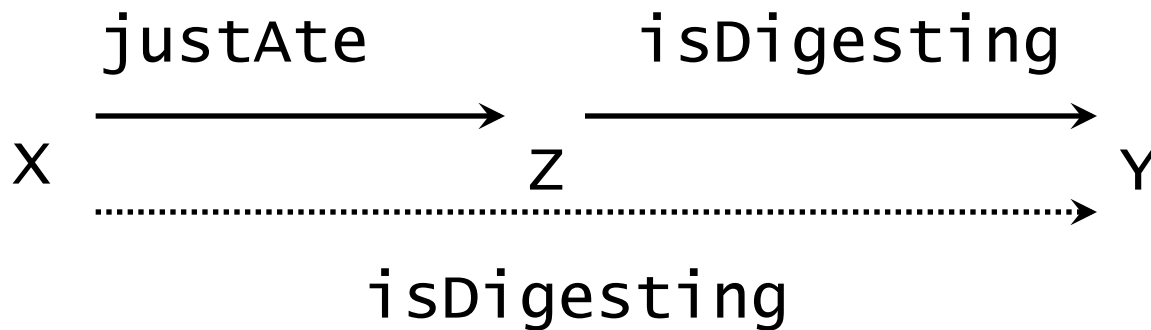
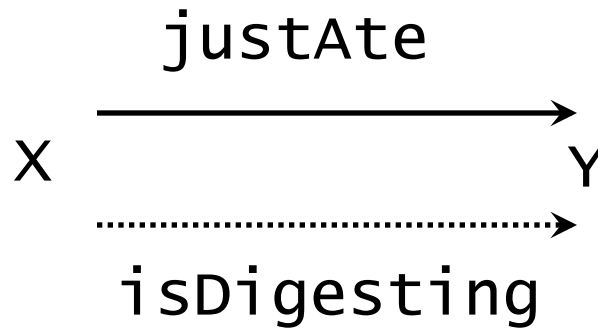
```
justAte(stork,frog).
```

```
?-
```

# Picture of the situation



# Picture of the situation



# Example 1: Eating

```
isDigesting(X,Y):- justAte(X,Y).
```

```
isDigesting(X,Y):- justAte(X,Z), isDigesting(Z,Y).
```

```
justAte(mosquito,blood(john)).
```

```
justAte(frog,mosquito).
```

```
justAte(stork,frog).
```

```
?- isDigesting(stork,mosquito).
```



# Example 1: Eating

isDigesting(X,Y):- justAte(X,Y).

isDigesting(X,Y):- justAte(X,Z), isDigesting(Z,Y).

justAte(mosquito,blood(john)).

justAte(frog,mosquito).

justAte(stork,frog).

?- isDigesting(stork,mosquito).

yes

?-

# Another recursive definition

p:- p.

?-

# Another recursive definition

p:- p.

?- p.

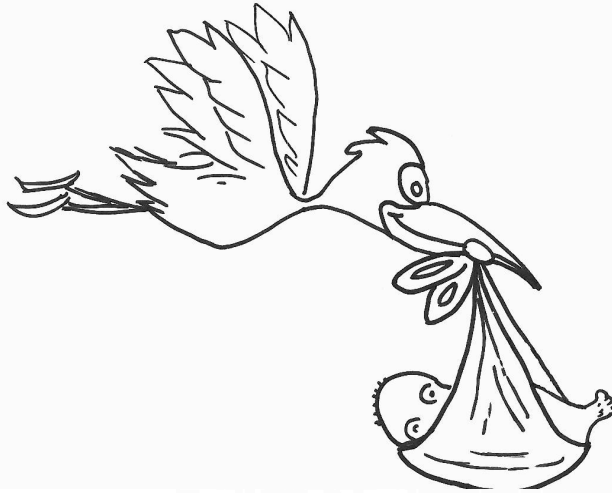
# Another recursive definition

p:- p.

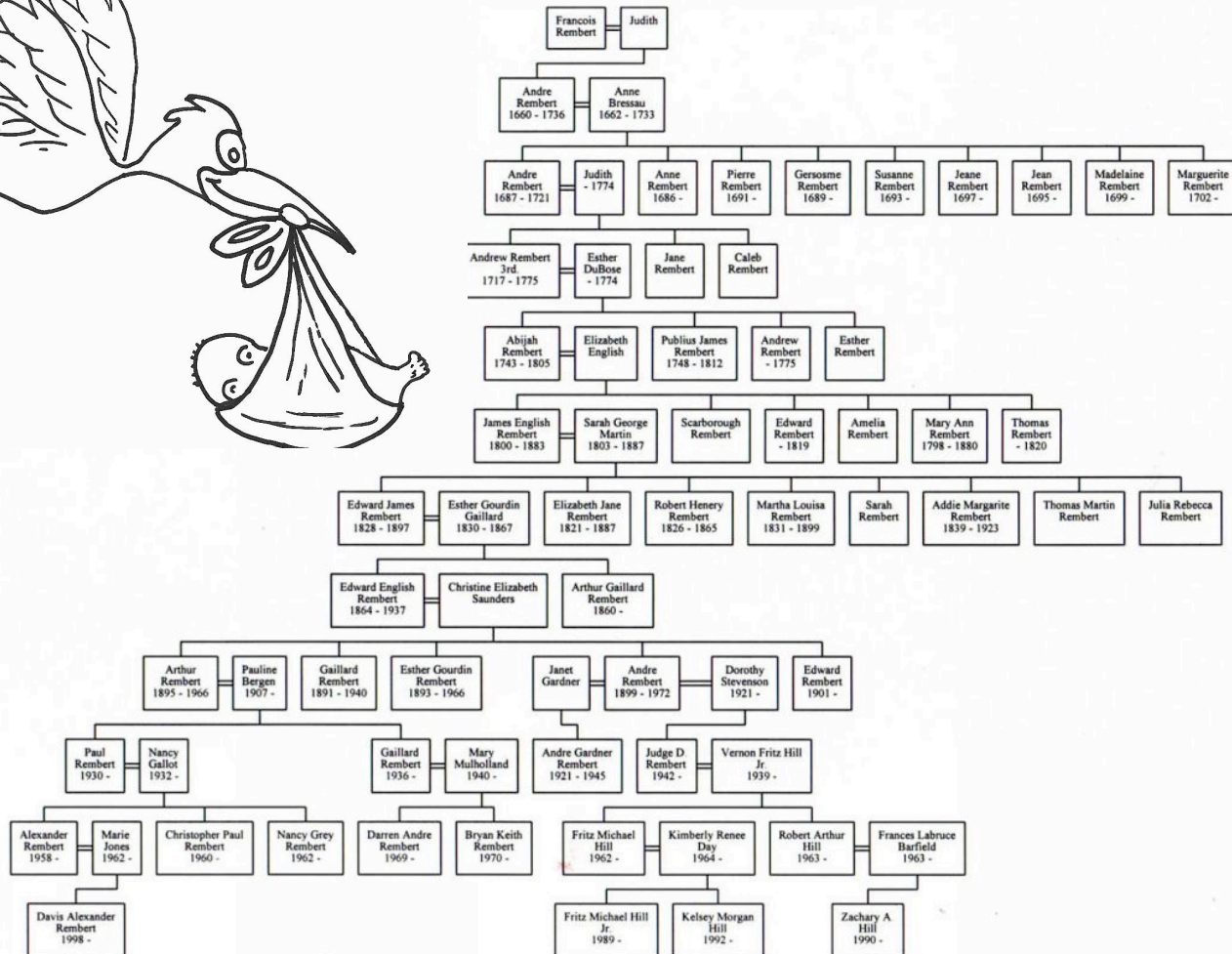
?- p.

ERROR: out of memory

# Example 2: Decendant



*Descendants of Francois Rembert*



# Example 2: Decendant

```
child(bridget,caroline).
```

```
child(caroline,donna).
```

```
descend(X,Y):- child(X,Y).
```

```
descend(X,Y):- child(X,Z), child(Z,Y).
```

# Example 2: Decendant

```
child(anna,bridget).
```

```
child(bridget,caroline).
```

```
child(caroline,donna).
```

```
child(donna,emily).
```

```
descend(X,Y):- child(X,Y).
```

```
descend(X,Y):- child(X,Z), child(Z,Y).
```

# Example 2: Decendant

```
child(anna,bridget).
```

```
child(bridget,caroline).
```

```
child(caroline,donna).
```

```
child(donna,emily).
```

```
descend(X,Y):- child(X,Y).
```

```
descend(X,Y):- child(X,Z), child(Z,Y).
```

```
?- descend(anna,donna).
```

```
no
```

```
?-
```



# Example 2: Decendant

```
child(anna,bridget).  
child(bridget,caroline).  
child(caroline,donna).  
child(donna,emily).
```

```
descend(X,Y):- child(X,Y).  
descend(X,Y):- child(X,Z), child(Z,Y).  
descend(X,Y):- child(X,Z), child(Z,U), child(U,Y).
```

?-

# Example 2: Decendant

```
child(anna,bridget).
```

```
child(bridget,caroline).
```

```
child(caroline,donna).
```

```
child(donna,emily).
```

```
descend(X,Y):- child(X,Y).
```

```
descend(X,Y):- child(X,Z), descend(Z,Y).
```

```
?-
```

# Example 2: Decendant

```
child(anna,bridget).
```

```
child(bridget,caroline).
```

```
child(caroline,donna).
```

```
child(donna,emily).
```

```
descend(X,Y):- child(X,Y).
```

```
descend(X,Y):- child(X,Z), descend(Z,Y).
```

```
?- descend(anna,donna).
```

# Search tree

---

Draw search tree for

?- descend(anna,donna).

# Example 3: Successor

---



# Example 3: Successor

---

Suppose we use the following way to write numerals:

1. **0** is a numeral.
2. If **X** is a numeral, then so is **succ(X)**.

# Example 3: Successor

```
numeral(0).
```

```
numeral(succ(X)):- numeral(X).
```

# Example 3: Successor

```
numeral(0).  
numeral(succ(X)):- numeral(X).
```

```
?- numeral(succ(succ(succ(0)))).  
yes  
?-
```



# Example 3: Successor

```
numeral(0).  
numeral(succ(X)):- numeral(X).
```

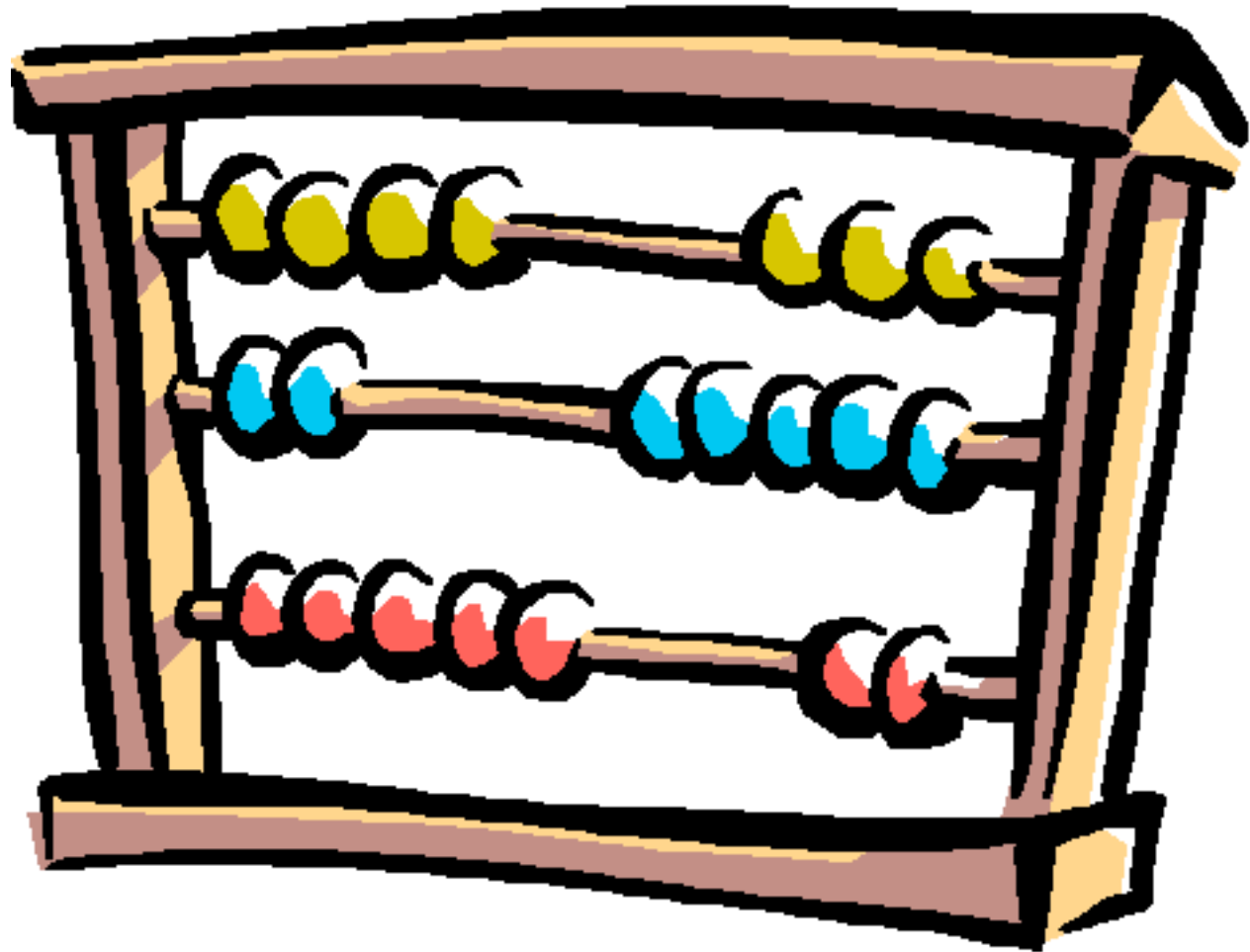
```
?- numeral(X).
```

# Example 3: Successor

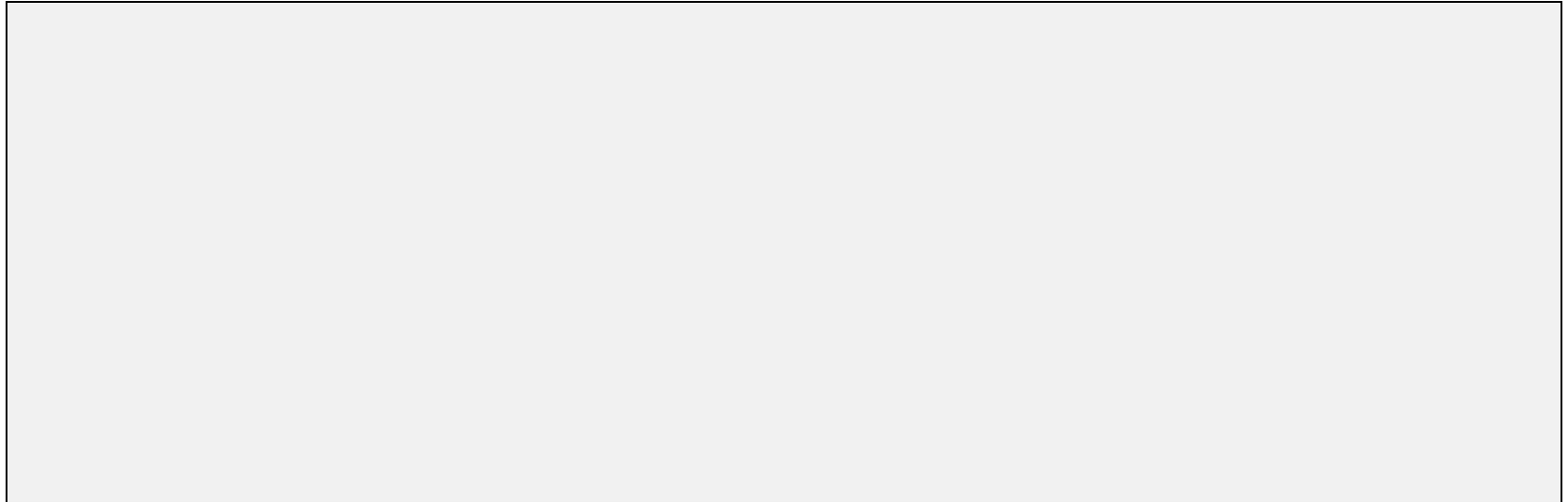
```
numeral(0).  
numeral(succ(X)):- numeral(X).
```

```
?- numeral(X).  
X=0;  
X=succ(0);  
X=succ(succ(0));  
X=succ(succ(succ(0)));  
X=succ(succ(succ(succ(0))))
```

# Example 4: Addition



# Example 4: Addition



?- add(succ(succ(0)),succ(succ(succ(0))), Result).

Result=succ(succ(succ(succ(succ(0))))))

yes

# Example 4: Addition

add(0,X,X).

%%% base clause

?- add(succ(succ(0)),succ(succ(succ(0))), Result).

Result=succ(succ(succ(succ(succ(0))))))

yes

# Example 4: Addition

```
add(0,X,X).                %%% base clause
```

```
add(succ(X),Y,succ(Z)):-  %%% recursive clause  
    add(X,Y,Z).
```

```
?- add(succ(succ(0)),succ(succ(succ(0))), Result).
```

```
Result=succ(succ(succ(succ(succ(0))))))
```

```
yes
```

# Search tree

Draw the  
search tree!



# Prolog and Logic

---

- Prolog was the first reasonable attempt to create a logic programming language
  - Programmer gives a declarative specification of the problem, using the language of logic
  - The programmer should not have to tell the computer what to do
  - To get information, the programmer simply asks a query

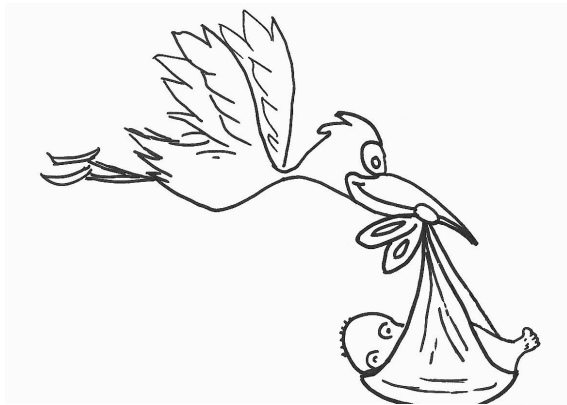


# Prolog and Logic

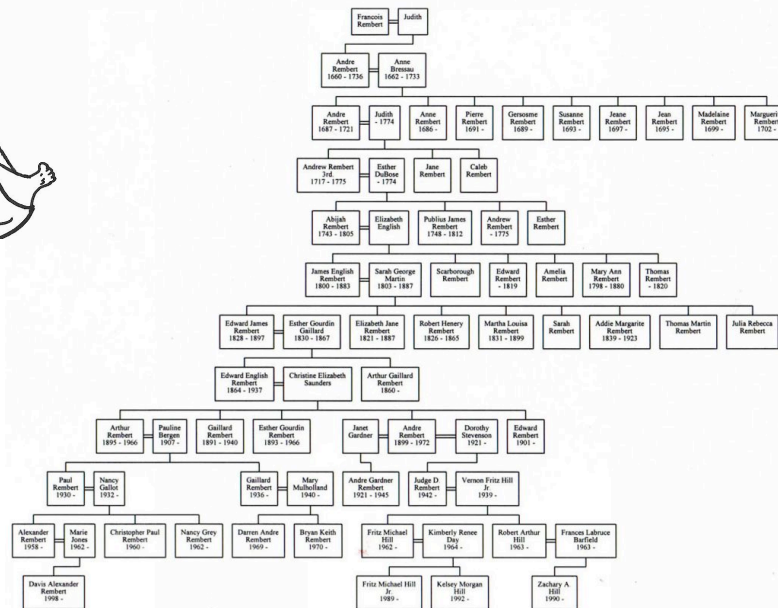
---

- Prolog does some important steps in this direction
- Nevertheless, Prolog is **not** a full logic programming language!
- Prolog has a specific way of answering queries:
  - Search knowledge base from top to bottom
  - Processes clauses from left to right
  - Backtracking to recover from bad choices

# Four different descend/2



Descendants of Francois Rember



# descend1.pl

```
child(anna,bridget).
```

```
child(bridget,caroline).
```

```
child(caroline,donna).
```

```
child(donna,emily).
```

```
descend(X,Y):- child(X,Y).
```

```
descend(X,Y):- child(X,Z), descend(Z,Y).
```

```
?- descend(A,B).
```

# descend1.pl

```
child(anna,bridget).
```

```
child(bridget,caroline).
```

```
child(caroline,donna).
```

```
child(donna,emily).
```

```
descend(X,Y):- child(X,Y).
```

```
descend(X,Y):- child(X,Z), descend(Z,Y).
```

```
?- descend(A,B).
```

```
A=anna
```

```
B=bridget
```

FIRST SOLUTION

# descend2.pl

```
child(anna,bridget).
```

```
child(bridget,caroline).
```

```
child(caroline,donna).
```

```
child(donna,emily).
```

```
descend(X,Y):- child(X,Z), descend(Z,Y).
```

```
descend(X,Y):- child(X,Y).
```

```
?- descend(A,B).
```

# descend2.pl

```
child(anna,bridget).
```

```
child(bridget,caroline).
```

```
child(caroline,donna).
```

```
child(donna,emily).
```

```
descend(X,Y):- child(X,Z), descend(Z,Y).
```

```
descend(X,Y):- child(X,Y).
```

```
?- descend(A,B).
```

```
A=anna
```

```
B=emily
```

FIRST SOLUTION

# descend3.pl

```
child(anna,bridget).
```

```
child(bridget,caroline).
```

```
child(caroline,donna).
```

```
child(donna,emily).
```

```
descend(X,Y):- descend(Z,Y), child(X,Z).
```

```
descend(X,Y):- child(X,Y).
```

```
?- descend(A,B).
```

# descend3.pl

```
child(anna,bridget).
```

```
child(bridget,caroline).
```

```
child(caroline,donna).
```

```
child(donna,emily).
```

```
descend(X,Y):- descend(Z,Y), child(X,Z).
```

```
descend(X,Y):- child(X,Y).
```

```
?- descend(A,B).
```

```
ERROR: OUT OF LOCAL STACK
```



# descend4.pl

```
child(anna,bridget).
```

```
child(bridget,caroline).
```

```
child(caroline,donna).
```

```
child(donna,emily).
```

```
descend(X,Y):- child(X,Y).
```

```
descend(X,Y):- descend(Z,Y), child(X,Z).
```

```
?- descend(A,B).
```

HOW MANY SOLUTIONS WILL THIS  
QUERY GENERATE BEFORE  
RUNNING OUT OF MEMORY?

# Summary of this lecture

---

- In this lecture we introduced recursive predicates
- We also looked at the differences between the declarative and the procedural meaning of Prolog programs
- We have identified some of the shortcomings of Prolog seen as a logical programming language

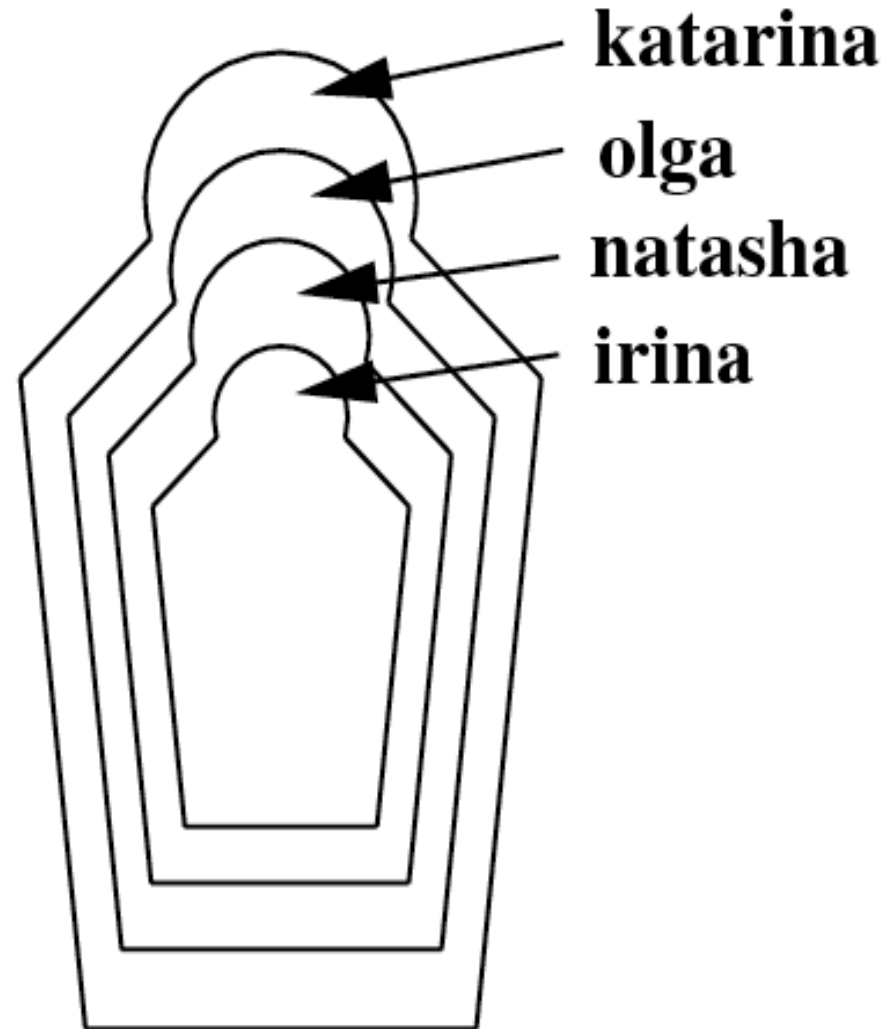
# Exercise 3.2: Matryoshka dolls



# Exercise 3.2: Matryoshka dolls

First, write a knowledge base using the predicate `directlyIn/2` which encodes which doll is directly contained in which other doll.

Then, define a recursive predicate `in/2`, that tells us which doll is (directly or indirectly) contained in which other dolls.



# Next lecture

---

- Introduce **lists** in Prolog
  - Important recursive data structure in Prolog programming
  - Define the `member/2` predicate, a fundamental Prolog tool for working with lists
  - Discuss the idea of recursing down lists