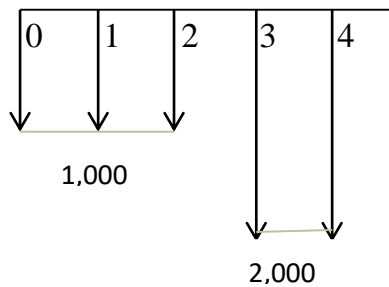


Tutorial 3

1- How many years from now the value of the given cash flow diagram will be equal to \$20,000? Interest rate is 10% per year.



Solution:

$$P(0) = 1,000 + 1,000 * (P/A, 10\%, 2) + 2,000 * (P/A, 10\%, 2) * (P/F, 10\%, 2) = 5,603.9$$

$$F(n) = 20,000$$

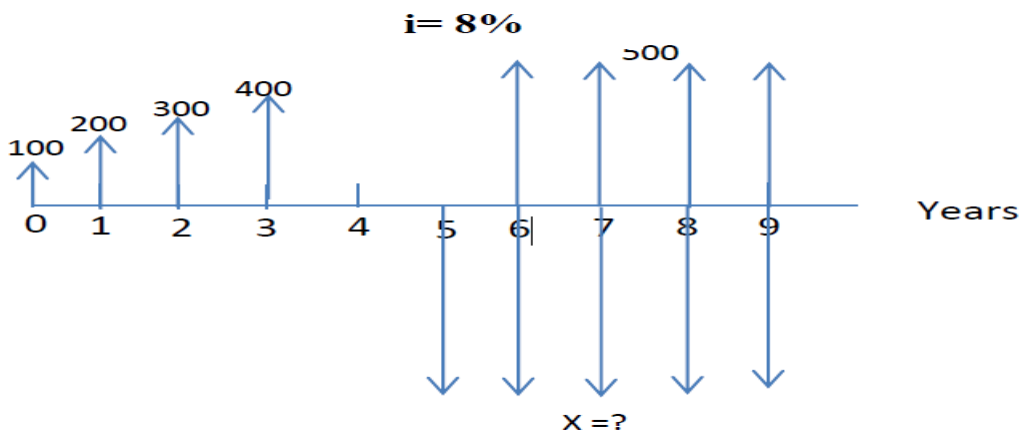
$$5,603.9 * (F/P, 10\%, n) = 20,000$$

$$5,603.9 * (1+0.1)^n = 20,000$$

$$(1.1)^n = 3.5689$$

$$n * \ln(1.1) = \ln(3.5689) \gg n = 13.34$$

2- Find the value of the unknown quantity in the cash flow diagram shown below, to establish equivalences of cash inflows and outflows ($i = 8\%$).



Since cash inflows and outflows are equivalent, their values are equal at a given time for example in your -1.

$$100(P/A, 8\%, 4) + 100(P/G, 8\%, 4) + 500(P/A, 8\%, 4) * (P/F, 8\%, 6) = X (P/A, 8\%, 5) * (P/F, 8\%, 5)$$

$$X = 677.17$$

3- For an interest rate of 8% per year, determine:

- Effective interest rate per year if interest is compounded daily?
- Effective interest rate semiannually if interest is compounded daily?
- Effective interest rate per year if interest is compounded monthly?
- Effective interest rate semiannually if interest is compounded every six months?

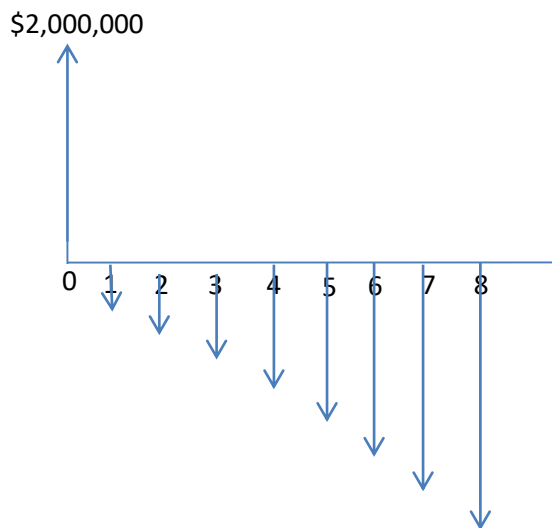
a) Effective i /year $= (1 + \frac{r}{m})^m - 1 = (1 + \frac{0.08}{365})^{365} - 1 = 8.33\%$

b) Effective i /semi-annually $= (1 + \frac{r}{m})^m - 1 = (1 + \frac{0.04}{182.5})^{182.5} - 1 = 4.081\%$

c) Effective i /year $= (1 + \frac{0.08}{12})^{12} - 1 = 8.29\%$

d) Effective i / semi-annually $= (1 + \frac{0.04}{1})^1 - 1 = 4\%$

4- Fieldsaver technologies, a manufacturer of precision laboratory equipment, borrowed \$2 million to renovate one of its testing labs. The loan was repaid in 2 years through quarterly payments that increased by \$50,000 each time. At an interest rate of 3% per quarter, what was the size of the first quarterly payment?



Effective i /quarter $= (1 + \frac{r}{m})^m - 1 = (1 + \frac{0.03}{1})^1 - 1 = 3\%$

$2,000,000 = A (P/A, 3\%, 8) + 50,000 (P/G, 3\%, 8) \longrightarrow A = \$117,665$